

UPDATING INDIANA ANNUAL FOREST INVENTORY AND ANALYSIS PLOT DATA USING EASTERN BROADLEAF FOREST DIAMETER GROWTH MODELS^{1 2}

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Abstract—The Forest Inventory and Analysis (FIA) program of the North Central Research Station (NCRS), USDA Forest Service, has developed nonlinear, individual-tree, distance-independent annual diameter growth models. The models are calibrated for species groups and formulated as the product of an average diameter growth component and a modifier component. The regional models for the Eastern Broadleaf (Continental)—Province 222, defined by R.G. Bailey, are calibrated using periodic Forest Inventory and Analysis data within that ecoregion. Average annual diameter growth is the dependent variable. The independent variables include crown ratio, crown class, stand basal area larger than the subject tree, physiographic class, latitude, and longitude. North Central Forest Inventory and Analysis has begun implementing annual inventories in a number of states of the region. The diameter growth models have been applied to annual data from Indiana to test their effectiveness on an independent data set that was collected under a survey design that differs from the one on which the models were calibrated. The bias of estimates increased with increasing values of crown ratio and with decreasing values of crown class.

INTRODUCTION

The North Central Research Station has developed nonlinear, individual-tree, distance-independent annual diameter growth models formulated as the product of an average diameter growth component and a modifier component and calibrated for species groups (Lessard and others submitted). The models may be used in two ways: (1) to update information on FIA plots not visited in the current year as a method of eliminating any lag in estimates of current conditions; and (2) to predict future forest resources.

Regional diameter growth models were developed for species groups within two ecoregions, the Laurentian Mixed Forest and the Eastern Broadleaf Forest (Lessard and McRoberts, in preparation). The objective of this study is to apply the Eastern Broadleaf Forest regional models to an independent data set, Indiana annual FIA data, and analyze the prediction performance.

PROVINCE 222

The diameter growth models are calibrated on FIA data from the Eastern Broadleaf Forest (Continental)—Province 222, defined by Bailey (1995). Province 222 is a subdivision of the Hot Continental Division. Most precipitation in Province 222 occurs during the growing season and generally decreases in quantity as distance from the Atlantic Ocean increases. This province favors drought-resistant oak-hickory associations. Province 222 lies to the east of the prairie regions, south and west of the Laurentian Mixed Forest—Province 212 in the northern areas, and west of the Appalachian Mountains in the southern regions. It extends from the Minnesota/Canadian border in the north through Missouri and Tennessee in the south.

CALIBRATION DATA

The diameter growth models were calibrated using FIA data across all ownership categories on land classified as timberland. Timberland was defined as non-reserved forestland that is producing or is capable of producing 20 ft²/ac/yr of industrial wood. The FIA periodic 10-point cluster survey design and the data collection were described by Hansen and others (1992). ArcView GIS was used to overlay Bailey's eco-region map (Bailey and others 1994) on the FIA plot locations to select plots within Province 222. Growth models were calibrated using FIA data from the following states (the parentheses refer to the year of the inventory): Michigan (1980, 1993), Wisconsin (1983, 1996), Minnesota (1990, 1993), Illinois (1985, 1998), Indiana (1986, 1998), Iowa (1974, 1990), Ohio (1978, 1990), Missouri (1972, 1989), Kentucky (1974, 1987), and Tennessee (1989, 1996).

INDIANA ANNUAL DATA

Data from both the old periodic 10-point cluster design and the new 4-point annual design plots were collected during the last periodic inventory in Indiana (1998). The new standard plot design is a cluster of four fixed-area subplots (24-foot radius) superimposed on four fixed-area micro-plots (6.8-ft radius). All trees 5.0 in dbh and larger are measured on the subplots and all trees 1.0-4.9 in dbh are measured on the micro-plots. Under the annual system, plots to be measured in each cycle are divided into five sub-cycles. Each sub-cycle is inventoried in a single year to complete the full inventory cycle in five years.

Two measurement intervals were included in the Indiana annual data set: (1) 1,358 trees (69 plots) in the 1998-1999 data (the last periodic, cycle 4 to cycle 5, sub-cycle 1); and (2) 1,503 trees (63 plots) in the 1998-2000 data (the last periodic, cycle 4 to cycle 5, sub-cycle 2).

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MODEL FORM

The form of the diameter growth model is:

$$E(\Delta DBH) = \text{AVERAGE} * \text{MODIFIER}, \text{ where} \quad (1a)$$

$$\text{AVERAGE} = \beta_1 \exp(-\beta_2 DBH) DBH^{\beta_3}, \text{ and} \quad (1b)$$

$$\text{MODIFIER} = \exp[\beta_4 (CR - 4) + \beta_5 (BAL - 50) + \beta_7 (CC - 3) + \beta_8 (PC - 5) + \beta_{10} (LNG - 89) + \beta_{11} ((LNG - 89)^2)/10 + \beta_{12} (LAT - 40) + \beta_{13} ((LAT - 40)^2)/10], \quad (1c)$$

where DBH is diameter at breast height, CR is crown ratio (percent of tree height consisting of crown), CC is crown class in five categories ranging from dominant to suppressed, BAL is plot basal area per acre for trees larger than that of the subject tree, PC is physiographic class coded in the data set as 3, 4, 5, 6, or 7 (corresponding with xeric, xeromesic, mesic, hydromesic, and hydric, respectively), LNG is longitude, and LAT is latitude. The modeling methodology and assessment of fit are documented in Lessard and others (in review).

BIAS ASSESSMENTS FOR MODELS APPLIED TO INDIANA ANNUAL DATA

Residual analysis was conducted to examine the adequacy of the diameter growth model predictions for an independent data set. The Eastern Broadleaf Forest regional models were applied to the FIA Annual Indiana data to obtain predicted diameter growth rates (in/yr) for individual trees. Predicted growth rates were compared to average annual observed change in DBH, calculated as the ratio of the difference in DBH at the two measurements and the number of years in the measurement interval. Residuals were calculated as differences between observed and predicted annual changes in diameter. To examine how well the models fit the data, percentile statistics (25th, 50th, 75th) were computed for the residuals by species group, and by classes of DBH, CR, BAL, CC, longitude, and latitude. Models were judged to be unbiased if zero was included in the range of values between the 25th and 75th percentiles for the residuals.

RESULTS AND CONCLUSIONS

The models were generally unbiased when the residuals were examined by species group (table 1), and by classes of DBH (table 2), CR (table 3), BAL (table 4), CC (table 5), LNG (table 6), and LAT (table 7). Several exceptions did occur. The models overestimated growth rates for cottonwood, however there were only 17 cottonwood trees in the data set used to test the models. Median residuals generally increased with increasing CR classes and with decreasing CC sizes. However, the inter-quartile range of residual values included zero for all but the largest and smallest classes of CR (table 3) and for the smallest CC with only 3 observations (table 5).

To examine the trend found in the residuals with respect to CR more closely, median average annual growth rates were calculated by CR class for both the Indiana Annual data and the Eastern Broadleaf Forest Periodic data and compared. Indiana Annual data growth rates were less than those of the calibration data for small CC values and greater for large CC

Table 1—Analysis of residuals (calculated as the observed minus predicted values) sorted by species group

| Species group | No. of trees | Percentile | | |
|-----------------------------|--------------|------------------|------------------|------------------|
| | | 25 th | 50 th | 75 th |
| | | In/yr | In/yr | In/yr |
| Softwoods | | | | |
| Eastern white pine | 36 | -0.117 | -0.031 | -0.003 |
| Red pine | 22 | -0.068 | -0.048 | 0.012 |
| Jack pine and Virginia pine | 93 | -0.022 | 0.037 | 0.099 |
| Shortleaf pine | 55 | -0.017 | 0.022 | 0.059 |
| Tamarack | 5 | -0.011 | 0.016 | 0.017 |
| Eastern redcedar | 100 | -0.026 | 0.021 | 0.111 |
| Other softwoods | 9 | -0.061 | -0.031 | 0.000 |
| Hardwoods | | | | |
| Select white oak | 158 | -0.065 | -0.027 | 0.018 |
| Other white oak | 32 | -0.063 | -0.031 | 0.046 |
| Northern red oak | 48 | -0.083 | -0.011 | 0.037 |
| Other red oak | 163 | -0.050 | 0.004 | 0.087 |
| Select hickory | 72 | -0.061 | -0.009 | 0.046 |
| Other hickory | 160 | -0.046 | -0.004 | 0.042 |
| Hard maple | 272 | -0.043 | -0.003 | 0.050 |
| Soft maple | 217 | -0.079 | -0.024 | 0.056 |
| Boxelder | 23 | -0.104 | -0.005 | 0.137 |
| American beech | 40 | -0.043 | -0.006 | 0.050 |
| White and green ash | 144 | -0.073 | -0.007 | 0.061 |
| Black ash | 7 | -0.102 | -0.052 | 0.014 |
| Aspen | 14 | -0.091 | 0.038 | 0.122 |
| Cottonwood | 17 | -0.182 | -0.097 | -0.035 |
| American basswood | 39 | -0.018 | 0.013 | 0.069 |
| Butternut and walnut | 77 | -0.057 | -0.014 | 0.053 |
| Black cherry | 153 | -0.084 | -0.014 | 0.075 |
| Elm | 168 | -0.060 | -0.005 | 0.060 |
| Hackberry | 28 | -0.056 | -0.015 | 0.089 |
| Sycamore | 27 | -0.110 | -0.040 | 0.014 |
| Yellow-poplar | 117 | -0.067 | 0.058 | 0.246 |
| Sweetgum | 35 | -0.026 | 0.032 | 0.113 |
| Tupelo | 40 | -0.046 | 0.002 | 0.071 |
| Sassafras | 125 | -0.059 | -0.029 | 0.006 |
| Flowering dogwood | 29 | -0.029 | -0.007 | 0.017 |
| Other commercial hardwoods | 68 | -0.089 | -0.025 | 0.064 |
| Noncommercial hardwoods | 69 | -0.033 | 0.010 | 0.066 |

Table 2—Analysis of residuals (calculated as the observed minus predicted values) sorted by 5-inch dbh class

| DBH class | Number of trees | Percentile | | |
|-----------|-----------------|------------------|------------------|------------------|
| | | 25 th | 50 th | 75 th |
| <i>In</i> | | <i>In/yr</i> | <i>In/yr</i> | <i>In/yr</i> |
| 1-5 | 228 | 0.061 | 0.004 | -0.041 |
| 5-10 | 1,502 | 0.064 | -0.006 | -0.055 |
| 10-15 | 606 | 0.064 | -0.002 | -0.054 |
| 15-20 | 213 | 0.032 | -0.030 | -0.082 |
| 20-25 | 83 | 0.082 | -0.023 | -0.096 |
| 25+ | 30 | 0.087 | -0.006 | -0.089 |

Table 3—Analysis of residuals (calculated as the observed minus predicted values) sorted by crown ratio

| Crown ratio class | Number of trees | Percentile | | |
|-------------------|-----------------|------------------|------------------|------------------|
| | | 25 th | 50 th | 75 th |
| <i>Percent</i> | | <i>In/yr</i> | <i>In/yr</i> | <i>In/yr</i> |
| 0-9 | 33 | -0.047 | -0.073 | -0.103 |
| 10-19 | 288 | 0.011 | -0.032 | -0.067 |
| 20-29 | 697 | 0.031 | -0.022 | -0.066 |
| 30-39 | 771 | 0.065 | -0.002 | -0.055 |
| 40-49 | 470 | 0.071 | -0.001 | -0.052 |
| 50-59 | 219 | 0.113 | 0.025 | -0.034 |
| 60-69 | 104 | 0.159 | 0.065 | 0.004 |
| 70-79 | 55 | 0.231 | 0.064 | -0.034 |
| 80-99 | 25 | 0.150 | 0.130 | 0.049 |

Table 4—Analysis of residuals (calculated as the observed minus predicted values) sorted by BAL

| BAL class | Number of trees | Percentile | | |
|--------------------------|-----------------|------------------|------------------|------------------|
| | | 25 th | 50 th | 75 th |
| <i>Ft²/ac</i> | | <i>In/yr</i> | <i>In/yr</i> | <i>In/yr</i> |
| 0-50 | 989 | -0.069 | -0.007 | 0.076 |
| 51-100 | 804 | -0.064 | -0.021 | 0.043 |
| 101-150 | 376 | -0.047 | -0.003 | 0.055 |
| 151-200 | 142 | -0.035 | 0.005 | 0.048 |
| 201-250 | 97 | -0.051 | -0.009 | 0.019 |
| 251-300 | 132 | -0.035 | 0.018 | 0.065 |
| 301-350 | 109 | -0.010 | 0.026 | 0.075 |
| 351-400 | 13 | 0.021 | 0.246 | 0.246 |

Table 5—Analysis of residuals (calculated as the observed minus predicted values) sorted by CC

| BAL class | Number of trees | Percentile | | |
|-----------|-----------------|------------------|------------------|------------------|
| | | 25 th | 50 th | 75 th |
| | | <i>In/yr</i> | <i>In/yr</i> | <i>In/yr</i> |
| 1 | 3 | 0.286 | 0.185 | 0.147 |
| 2 | 79 | 0.154 | 0.052 | -0.011 |
| 3 | 1,457 | 0.074 | 0.004 | -0.057 |
| 4 | 626 | 0.048 | -0.017 | -0.060 |
| 5 | 497 | 0.027 | -0.020 | -0.052 |

Table 6—Analysis of residuals (calculated as the observed minus predicted values) sorted by longitude

| Longitude | Number of trees | Percentile | | |
|----------------|-----------------|------------------|------------------|------------------|
| | | 25 th | 50 th | 75 th |
| <i>Degrees</i> | | <i>In/yr</i> | <i>In/yr</i> | <i>In/yr</i> |
| -87.55 | 230 | 0.076 | 0.004 | -0.051 |
| -87.05 | 364 | 0.066 | -0.005 | -0.063 |
| -86.55 | 1,066 | 0.041 | -0.013 | -0.057 |
| -86.05 | 301 | 0.085 | 0.012 | -0.043 |
| -85.55 | 405 | 0.080 | -0.005 | -0.058 |
| -85.05 | 296 | 0.072 | 0.005 | -0.067 |

Table 7—Analysis of residuals (calculated as the observed minus predicted values) sorted by latitude

| Latitude | Number of trees | Percentile | | |
|----------------|-----------------|------------------|------------------|------------------|
| | | 25 th | 50 th | 75 th |
| <i>Degrees</i> | | <i>In/yr</i> | <i>In/yr</i> | <i>In/yr</i> |
| 38.05 | 475 | 0.069 | 0.015 | -0.034 |
| 38.55 | 521 | 0.034 | -0.014 | -0.053 |
| 39.05 | 461 | 0.057 | -0.017 | -0.064 |
| 39.55 | 302 | 0.085 | 0.008 | -0.049 |
| 40.05 | 92 | 0.129 | 0.019 | -0.057 |
| 40.55 | 124 | 0.092 | -0.001 | -0.083 |
| 41.05 | 441 | 0.043 | -0.021 | -0.064 |
| 41.55 | 246 | 0.074 | -0.003 | -0.071 |

values. This follows the underestimation and overestimation patterns of the residuals (table 3).

In the context of their intended applications, the annual diameter growth models may be considered generally unbiased. However, because diameter growth rates with respect to CR tended to change from the time during which the calibration data were collected to the time the annual data was collected, exploration of methodology to capture these changes may improve the diameter growth predictions. Inclusion of climate variables in the model or application of model updating (e.g. Bayes) may improve the quality of diameter growth predictions.

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